



# How to Guggenheim the RFOFO Ring

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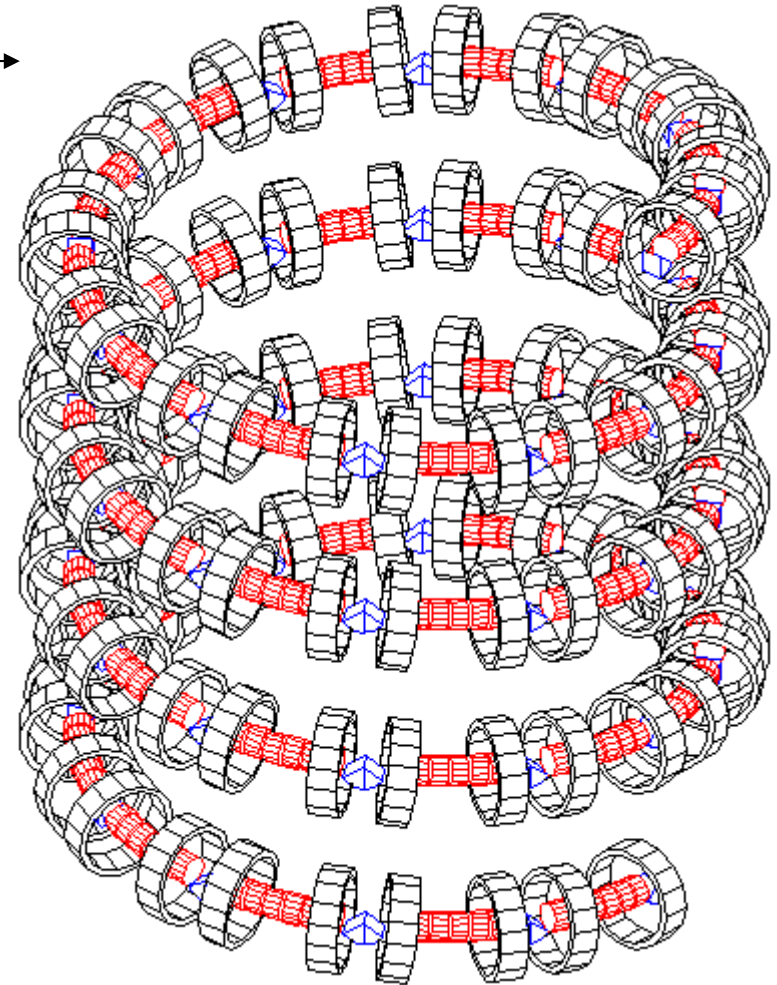
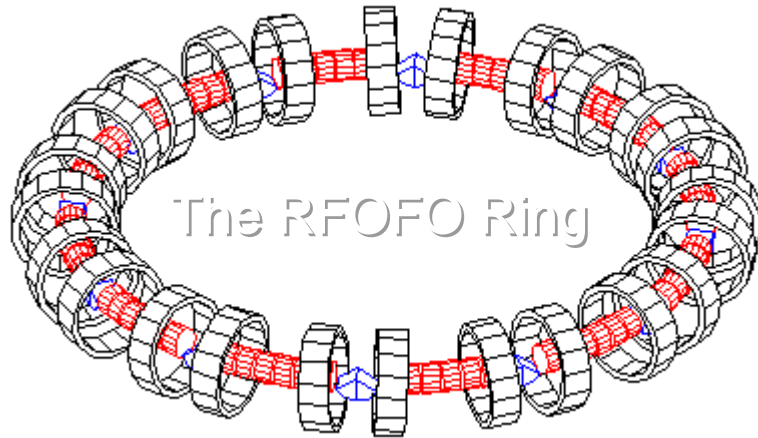
# Outline

- Why Guggenheim?
  - Geometric manipulations
  - “Shielding” studies
  - Some “Tapering” studies
- All very preliminary

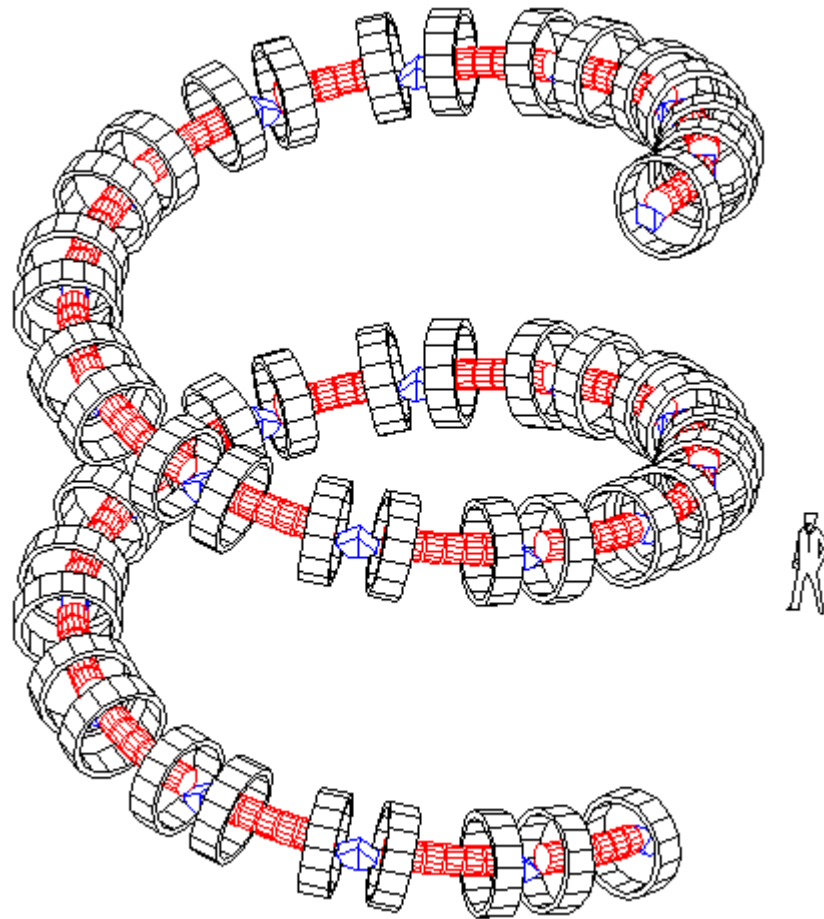
# The idea: change the geometry

from this ↓

to this →



# A simpler view of the Guggenheim



# Why “Guggenheim”?

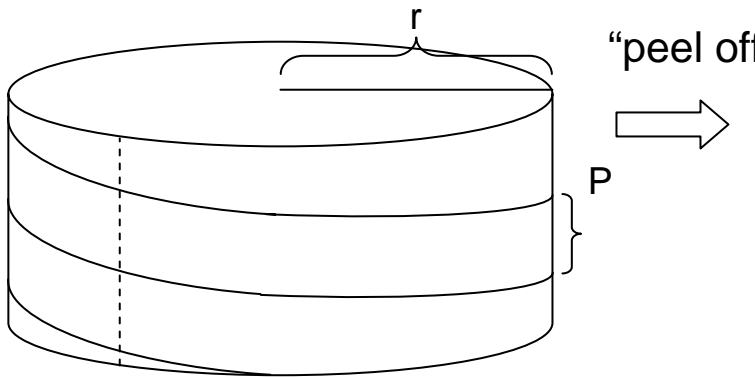
- Injection/extraction – not a problem!
- Unlimited bunch train length
- Less heating in the absorbers
- Tapering → more efficient cooling, cheaper  
BUT –
- massive, expensive (more RF cavities)
- Magnetic shielding of some sort is needed
- Can’t cool both signs in the same channel

# Simulating the Guggenheim ring

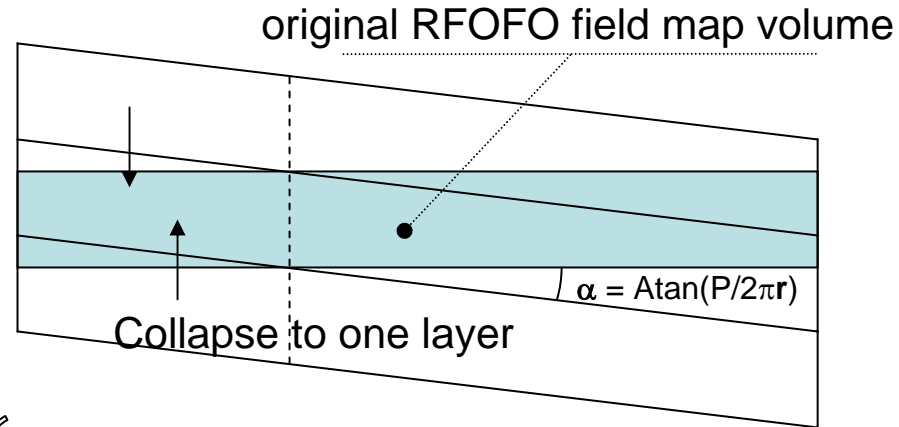
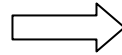
- Starting with:
  - a working GEANT3 simulation of the RFOFO
  - magnetic field map for the RFOFO ring
- Software modification:
  - Turning the existing field map into a “Guggenheim” using 2 parameters:  $P$  (pitch) and  $\phi_0$  (azimuthal angle offset)
  - This modification does not take into account the effects of “ring stacking”

# Turning a ring into a helix

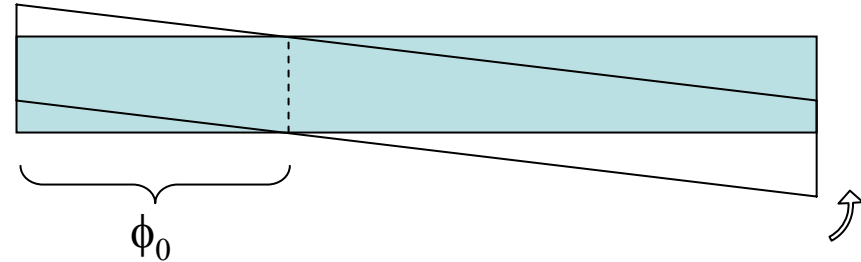
For each point  $x,y,z \rightarrow r,\phi,y$



"peel off"



Rotate by angle  $\alpha$

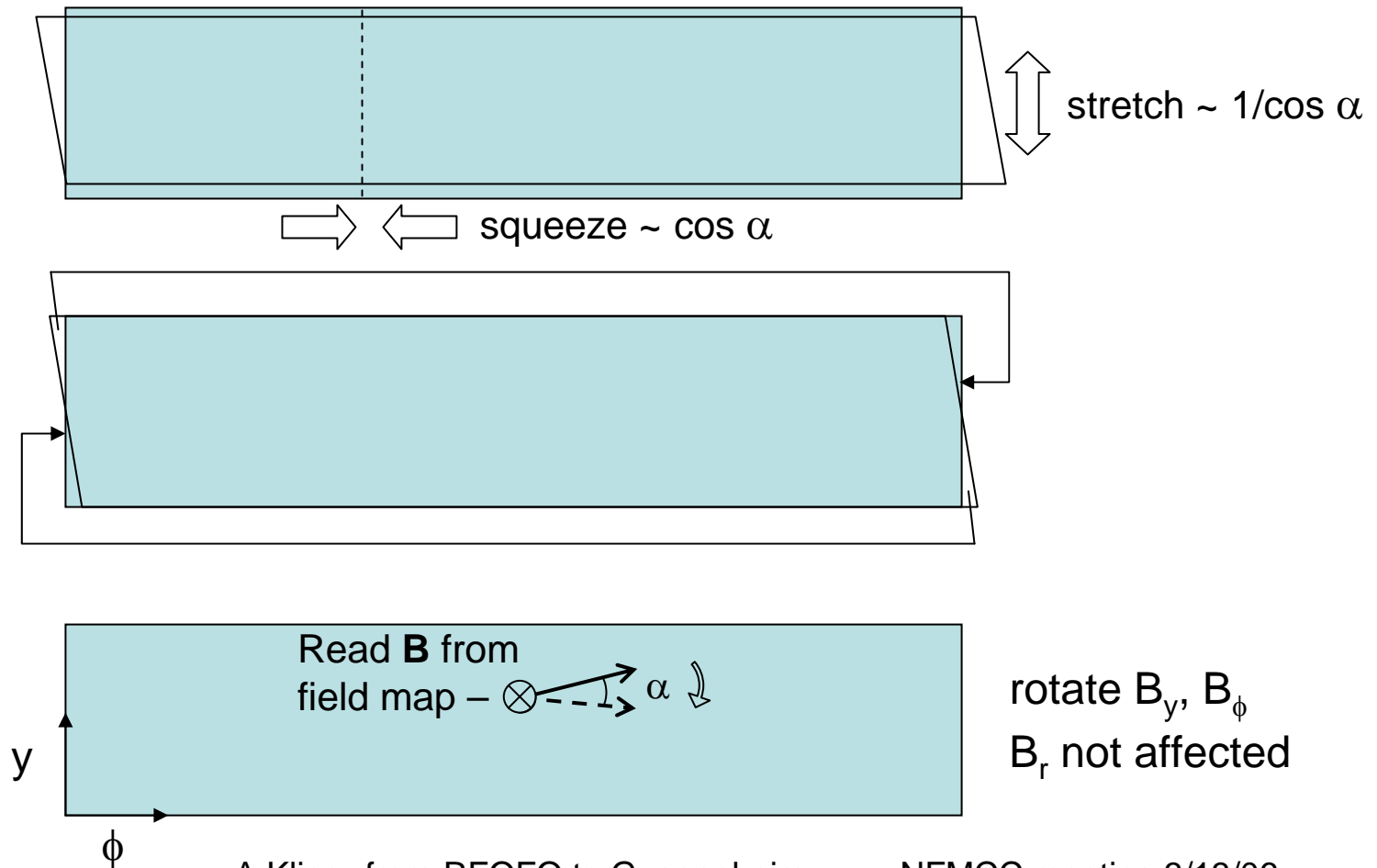


More adjustments needed



# Turning a ring into a helix

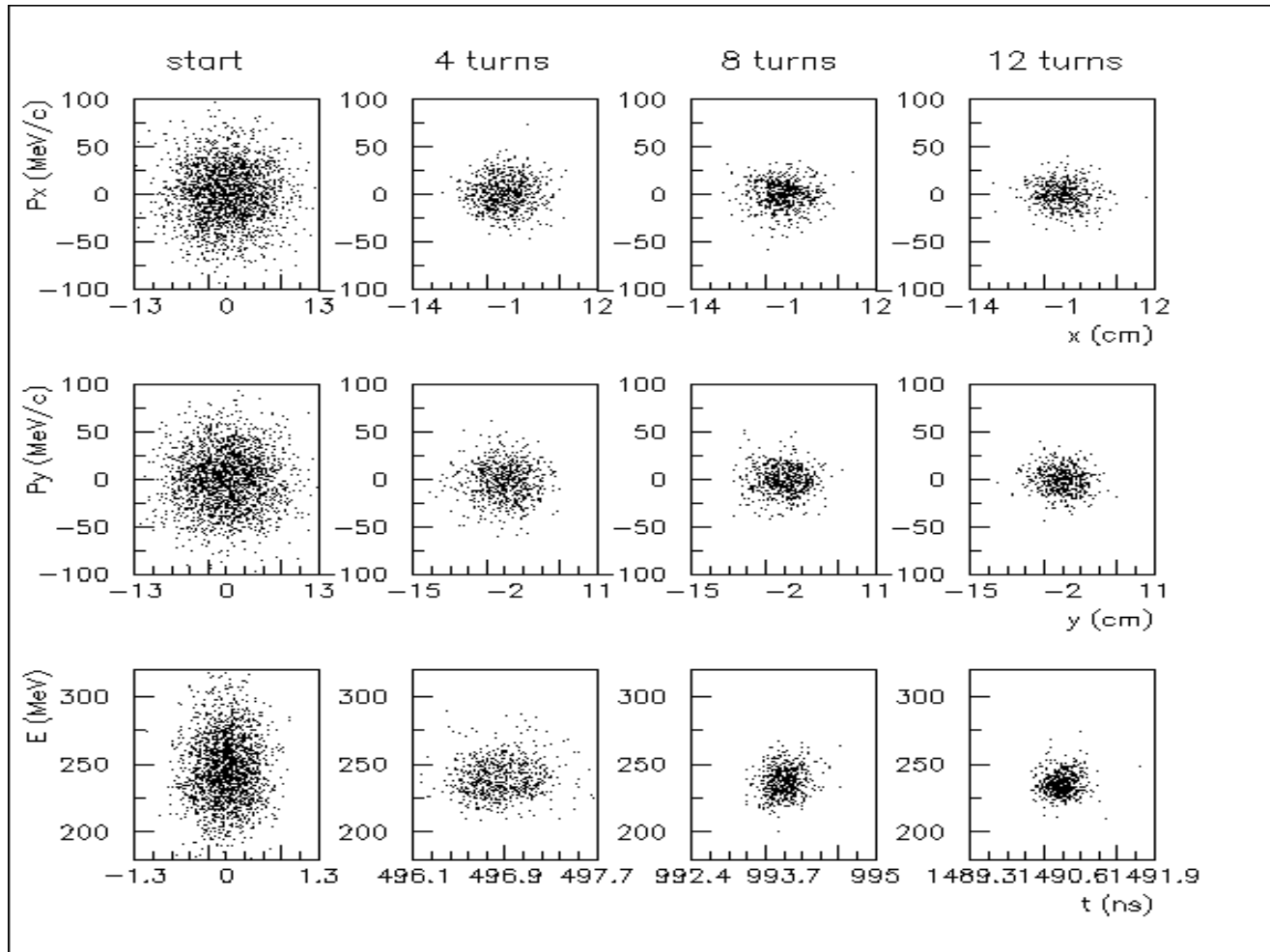
Exaggerated view of a single “slice”:



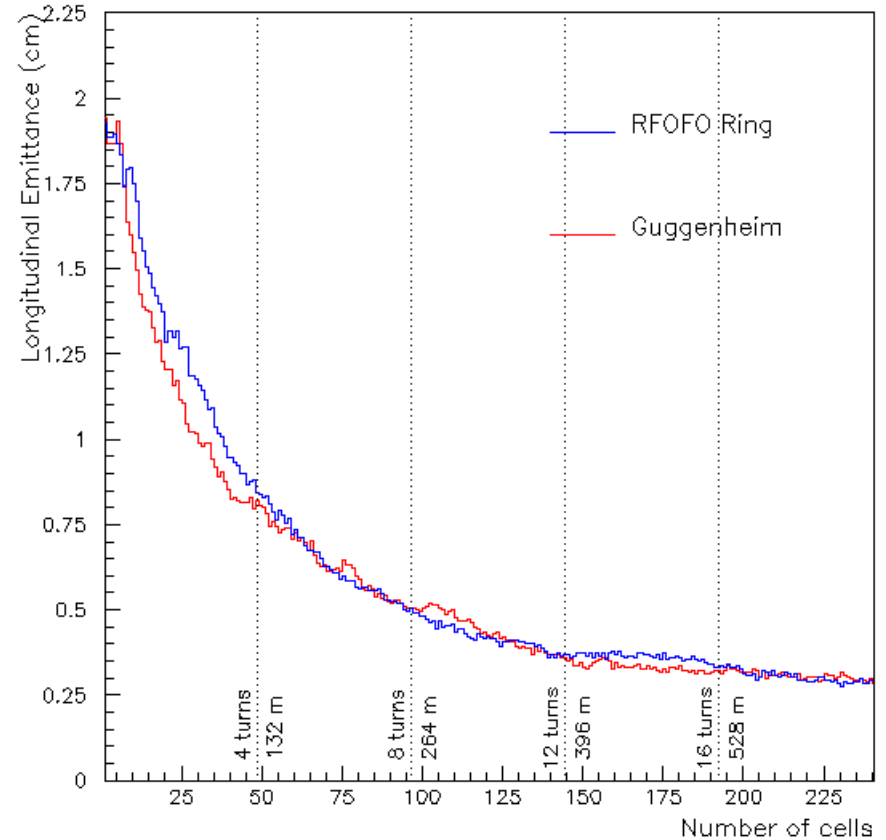
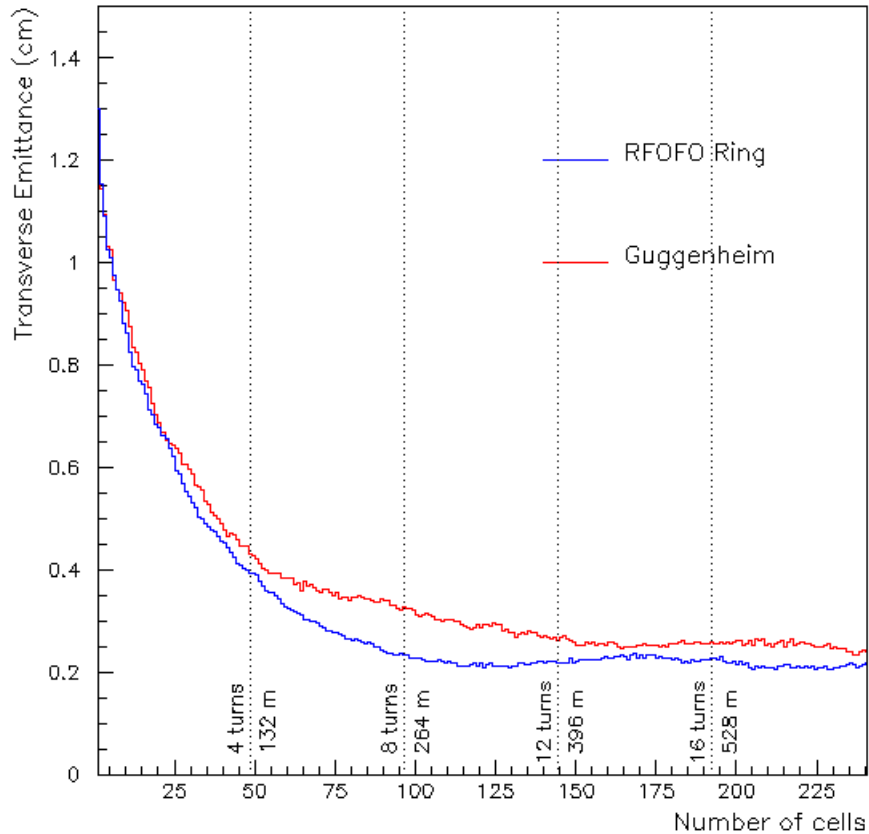
# Cooling simulation

- Pitch = 3 m
- No windows, but otherwise realistic...
- The “reference orbit” – 25<sup>th</sup> harmonic of the 201.25 MHz (**not necessary!**)
  - Longitudinal momentum = 205 MeV/c, compared to 201 MeV/c for RFOFO
    - (longer path requires  $\beta$  ratio =  $1/\cos \alpha(r)$ )
- Use the same 1000-muon beam as the RFOFO
  - rotate by angle  $\alpha$  about the x/r axis at entry

# Cooling... seems to work



# Comparing results

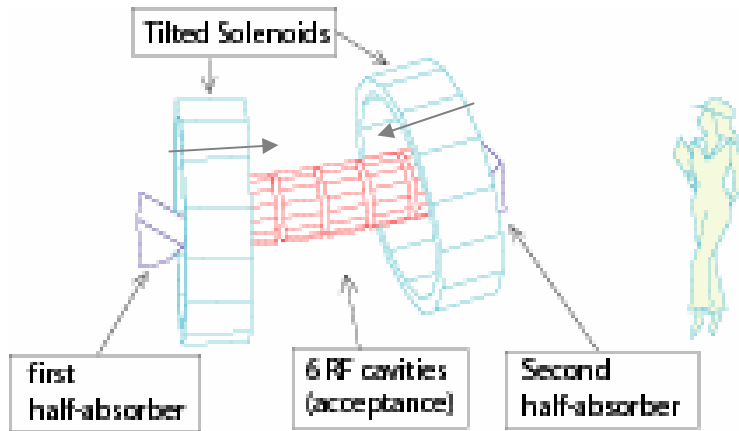


# “Guggenheiming” the RFOFO

- Works in principle
- More realistic magnetic fields needed
  - Will be done (hopefully) soon

# “Shielding” studies

The RFOFO cell:

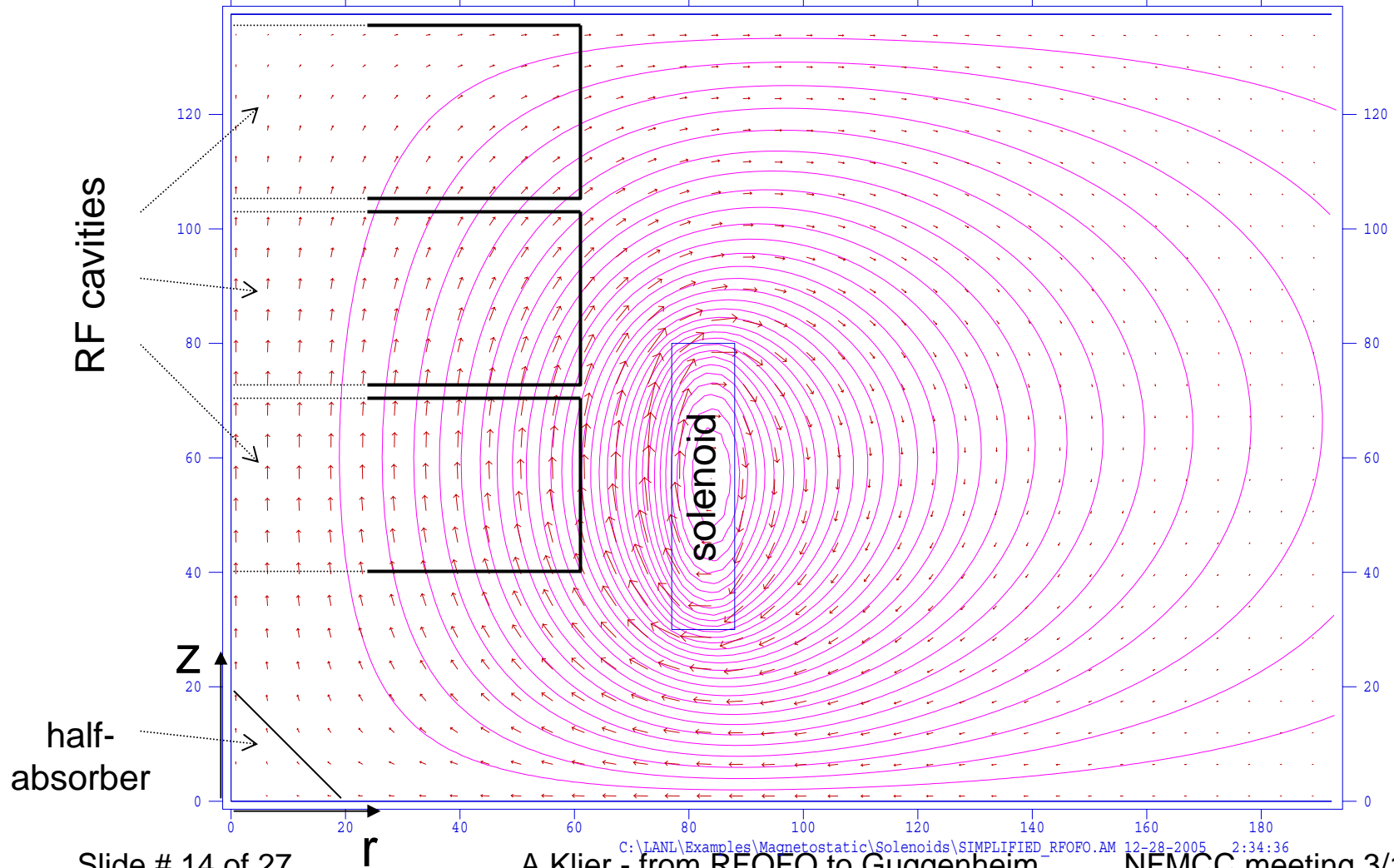


Simplified version:

- “Straighten” the cell (cancel solenoid tilt)  
→ 2-dim. problem ( $r, z$ )
- Cut in half (at field flip)
- Boundary conditions:  
 $B_z = 0$  at edges  
 $B_r = 0$  at  $r = 0$
- **“Iron” shielding:**  
 $\mathbf{B} \perp$  surface (i.e.  $B_z = 0$ )  
at  $r = R_{\text{shield}}$

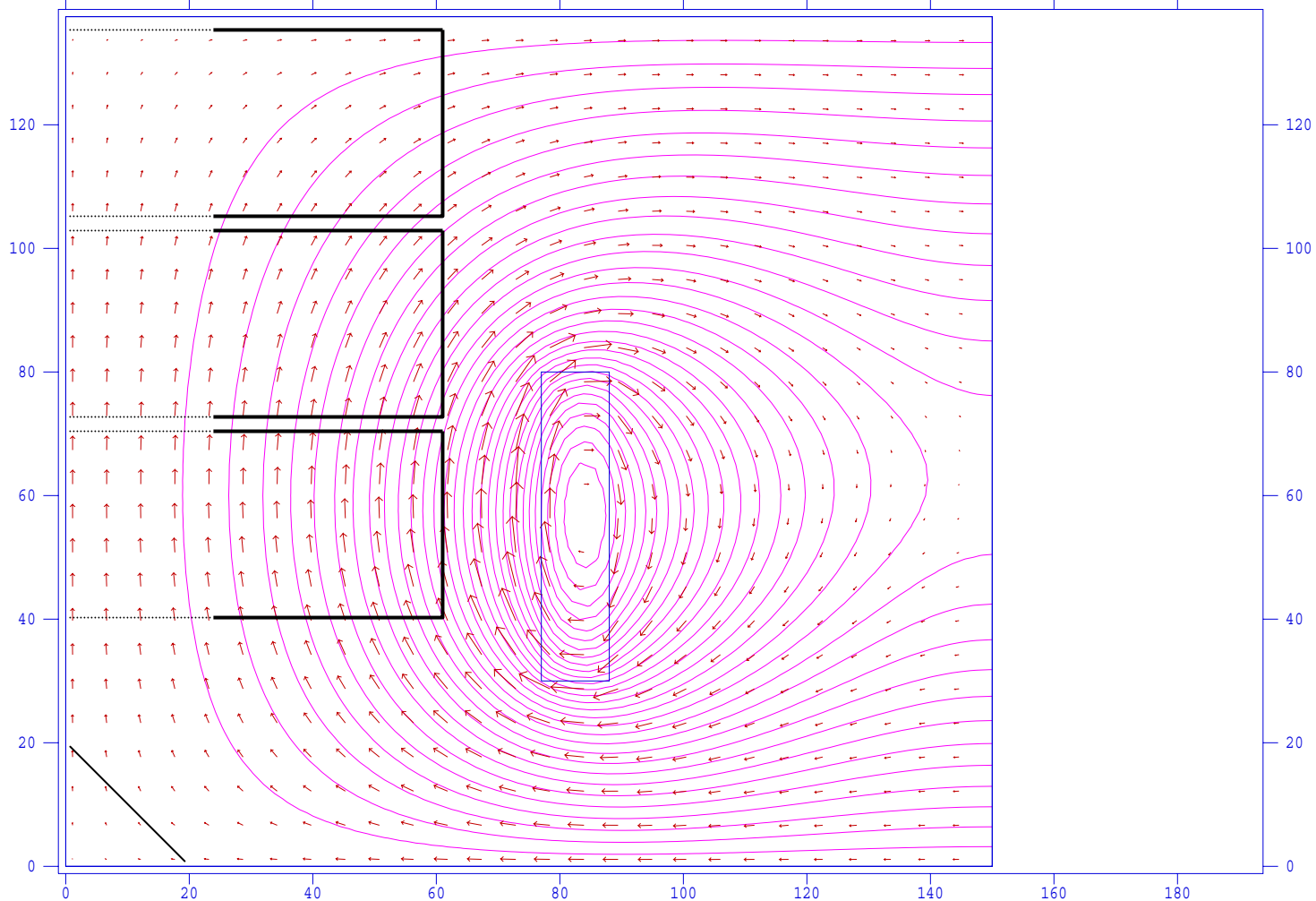
# B Field (Poisson-Superfish): No shielding

Simplified RFOFO Solenoid, no shielding



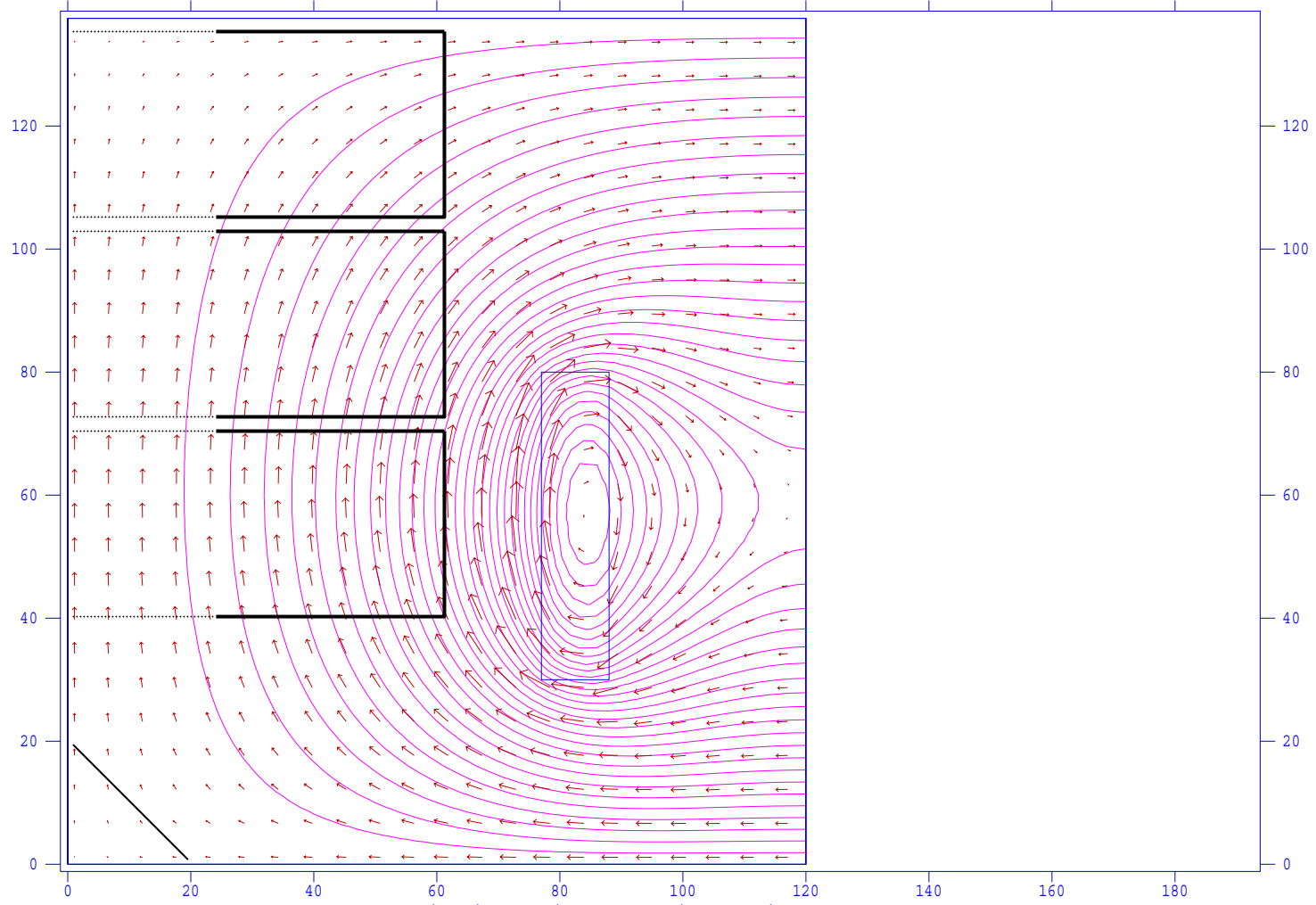
# Shielding at $r = 1.5$ m

Simplified RFOFO Solenoid



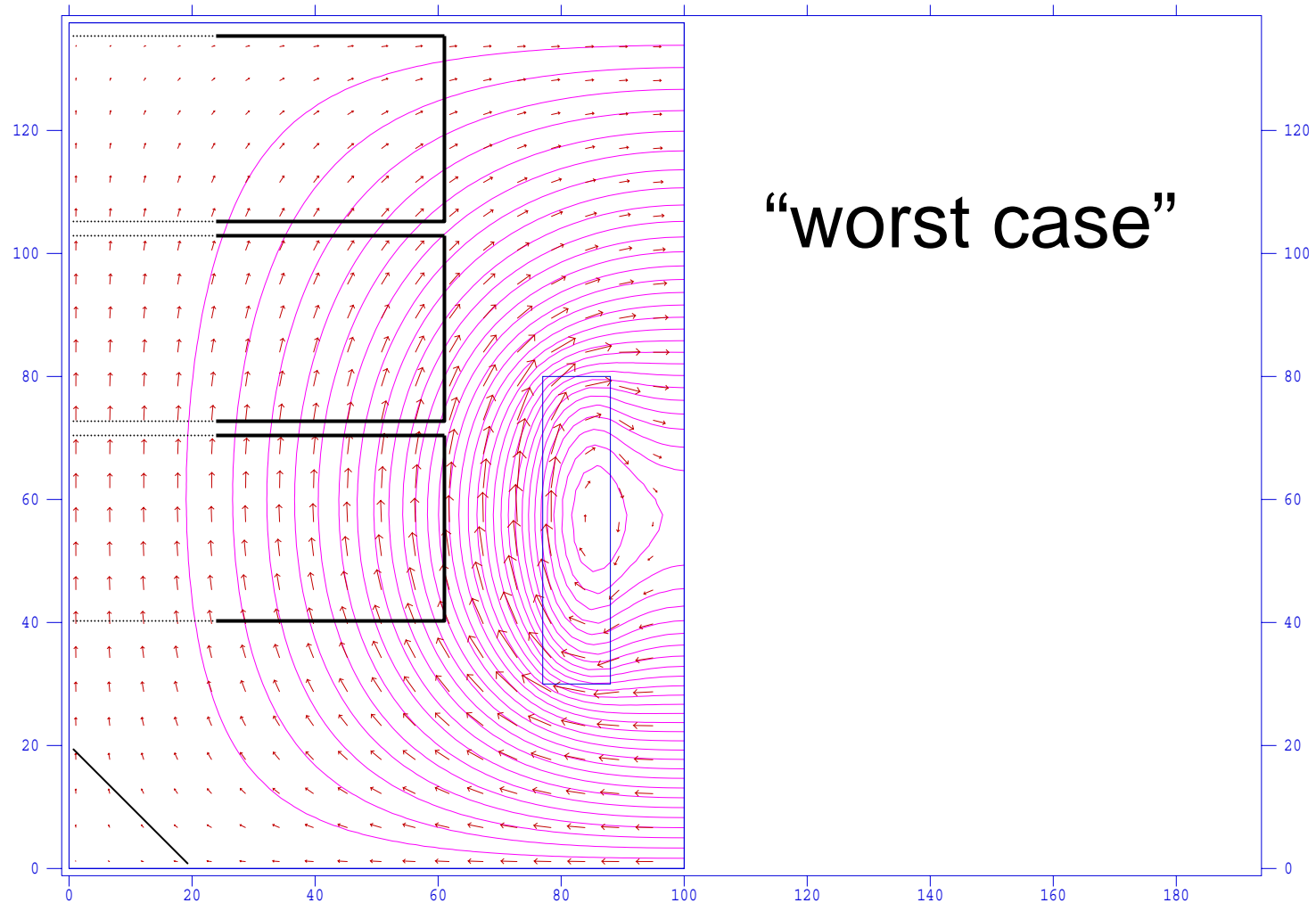
# Shielding at $r = 1.2$ m

Simplified RFOFO Solenoid

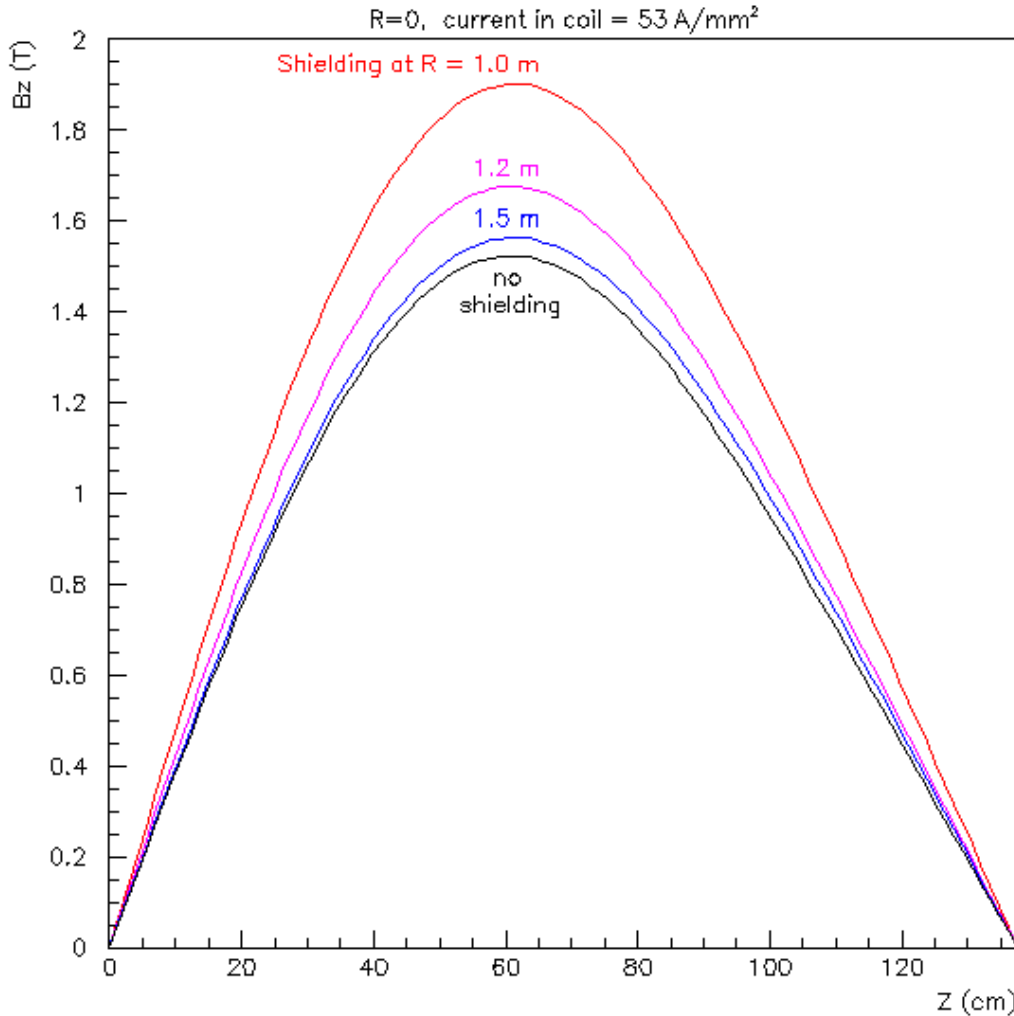


# Shielding at $r = 1.0$ m

Simplified RFOFO Solenoid



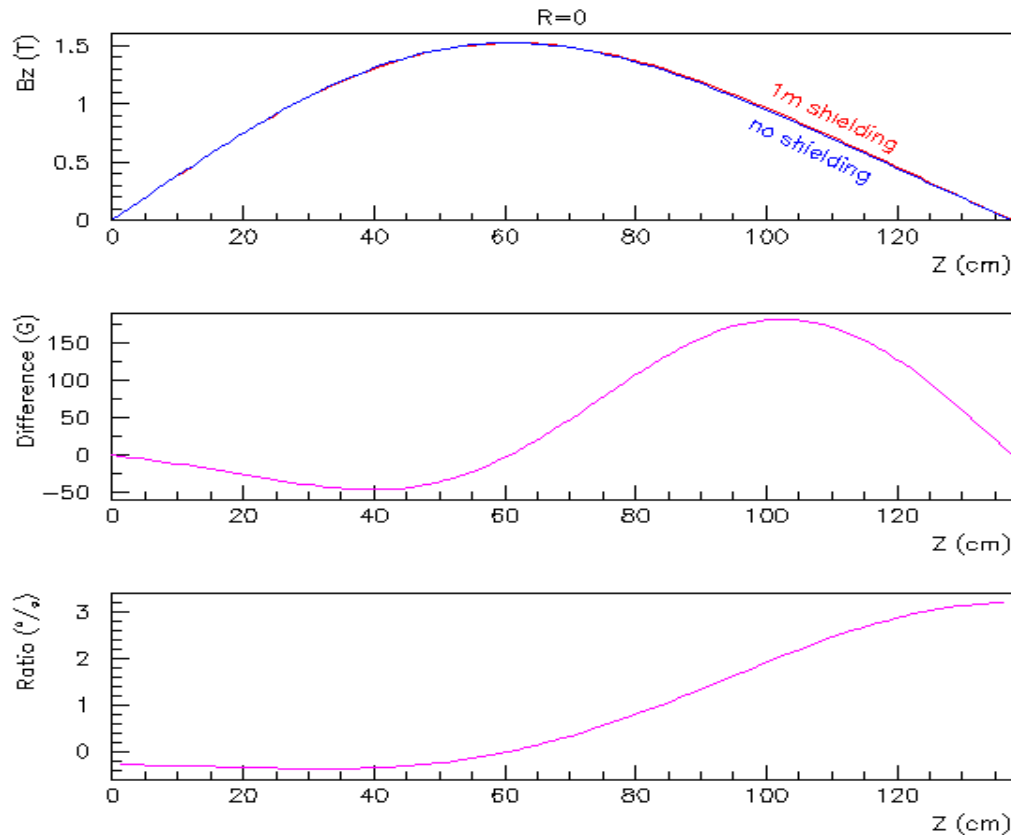
# Strength of B field at $r = 0$



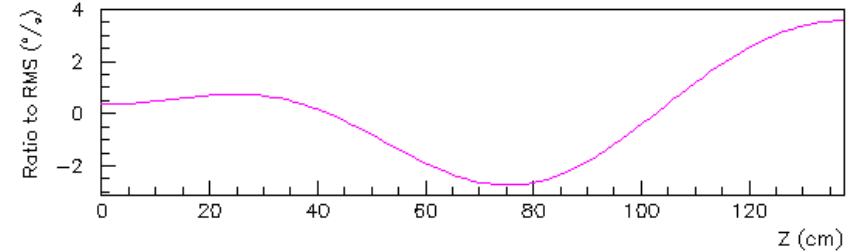
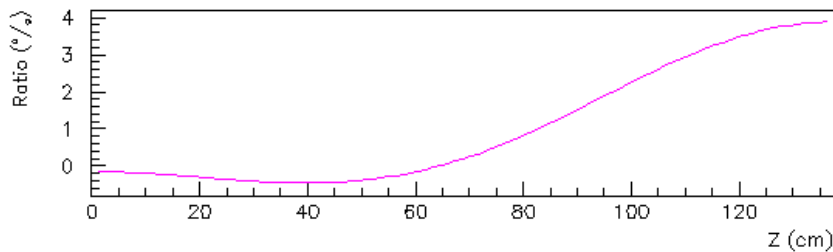
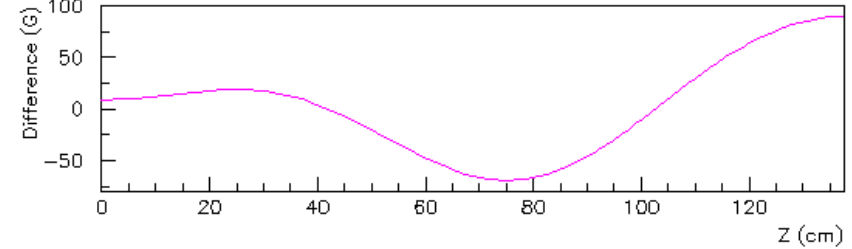
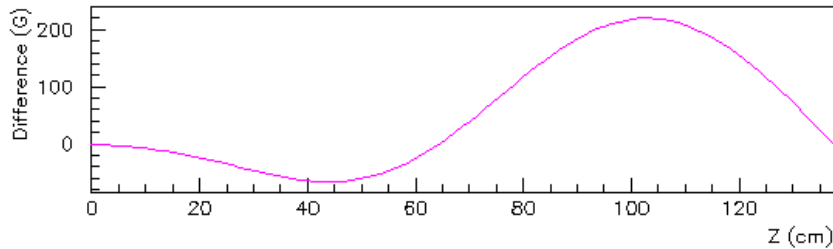
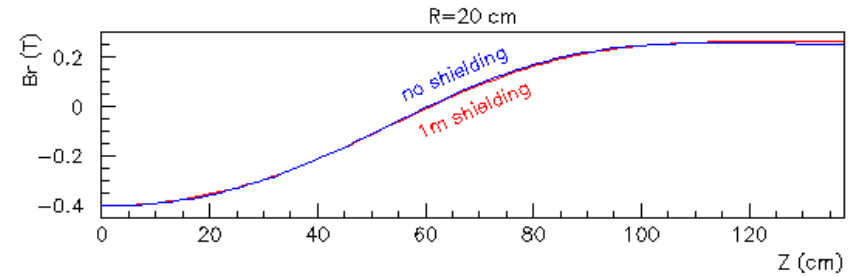
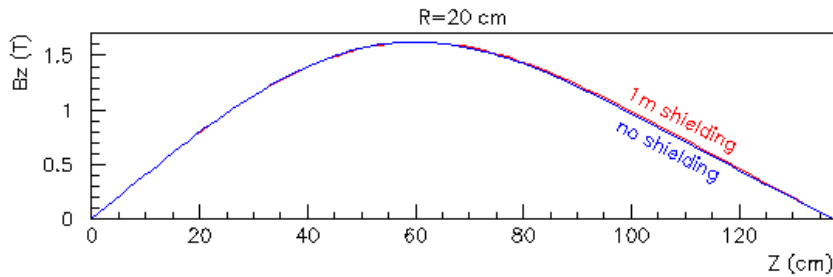
For the comparison I normalized the currents to match Bz maximum at  $r = 0$  without shielding

Shielding	Current (A/mm <sup>2</sup> )
none	53.00
1.5 m	51.66
1.2 m	48.18
1.0 m	42.47

# Comparing no shielding and “worst case” (normalized) at $r = 0$



# Comparing no shielding and “worst case” (norm.) at $r = 20$ cm

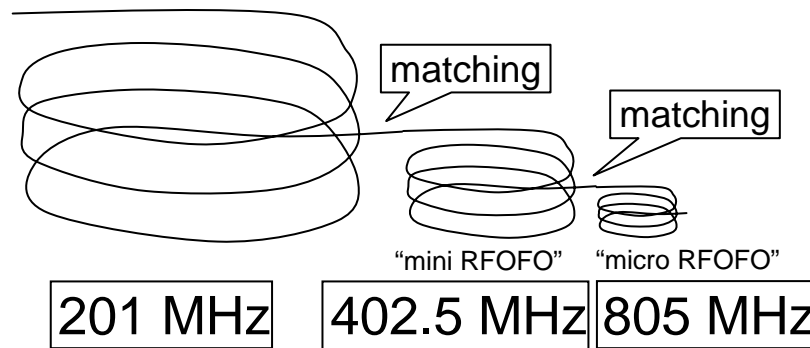


# “Shielding” studies

- Shielding seems to have little effect on magnetic field near the beam
- Forces, saturation, engineering design
  - Save it for later...
- Meanwhile we can simulate without iron and **not worry about it**

# “Tapering” studies (preliminary)

- Actually, it’s a 3-stage scheme:

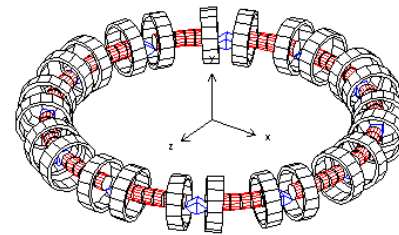
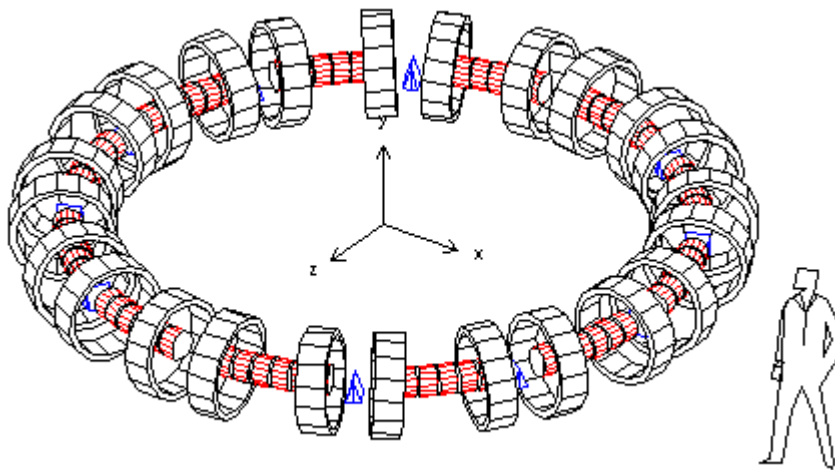


- The way I simulate (for now):
  - Use existing RFOFO (not “Guggenheim”) field
  - Scale geometry (1/2, 1/4), field, RF frequency
  - RF Gradient scales by about 1.5 each step

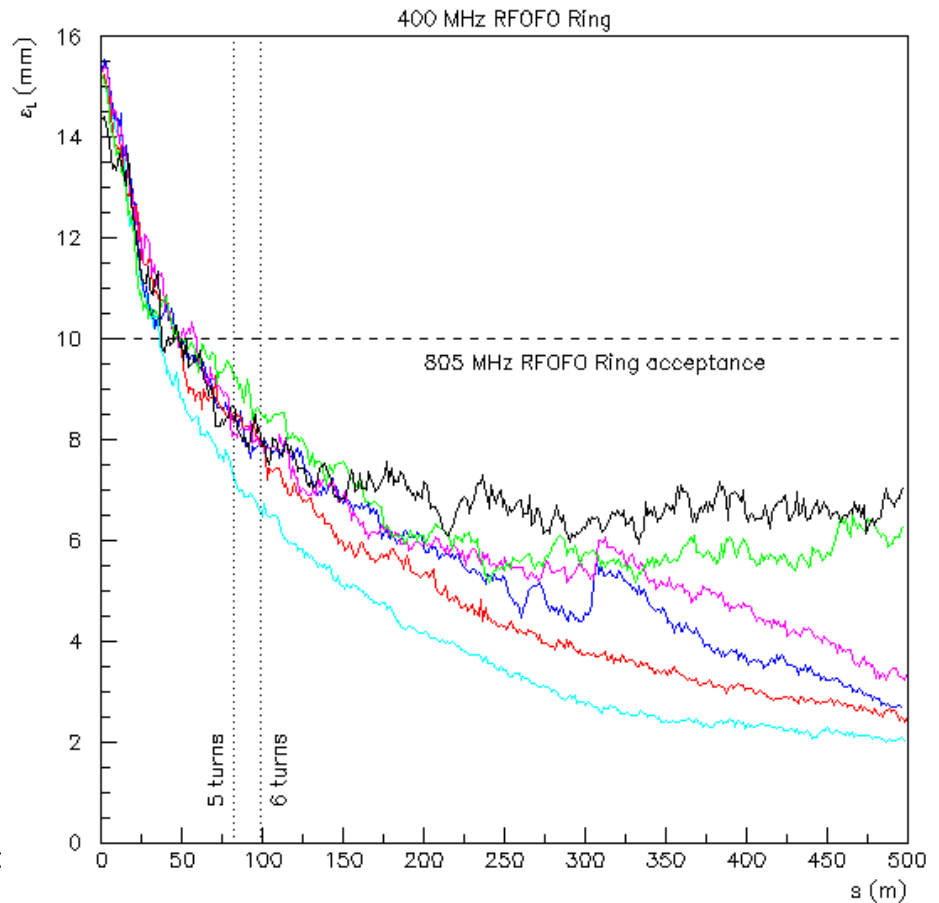
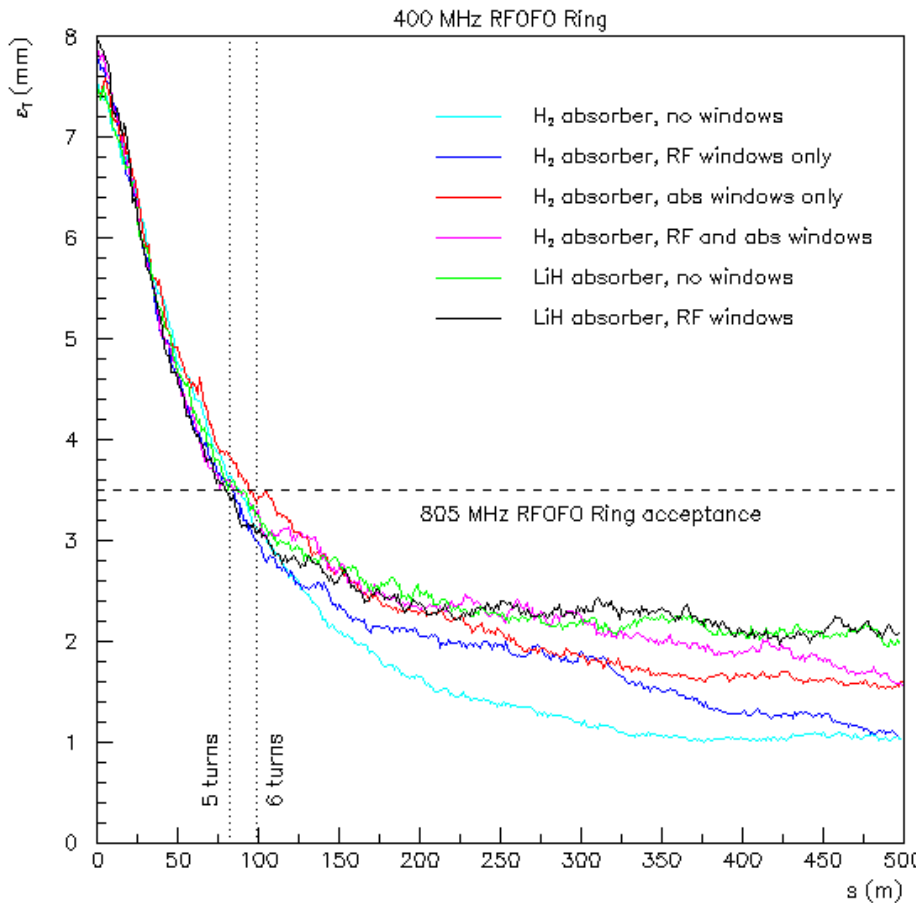
# Geometry

402.5 MHz ring

805 MHz ring

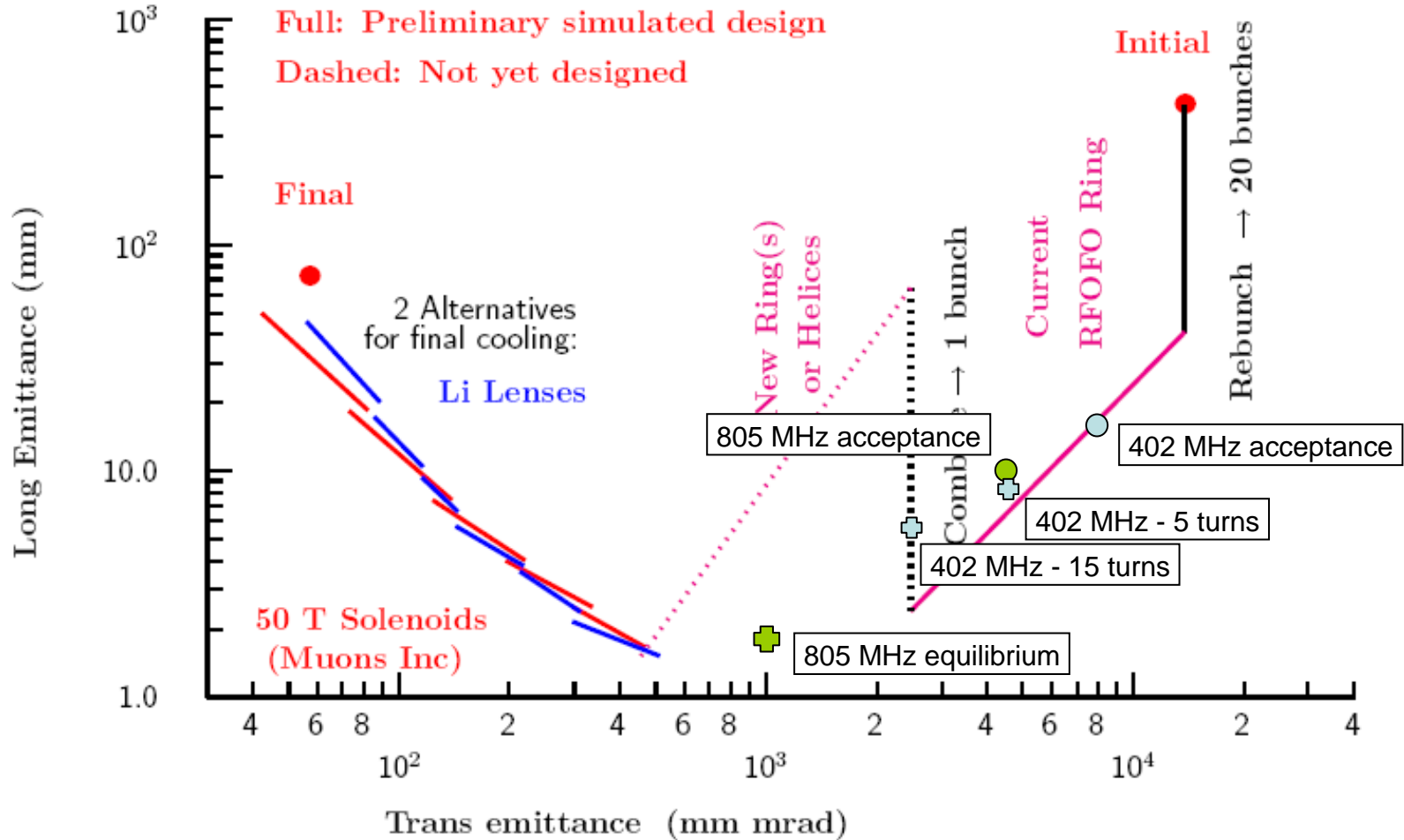


# Some results



# Roadmap to a muon collider

Bob Palmer's "grand scheme" (Friday meeting, 2/17/06)



# To do

- Simulate with “Guggenheim” instead of ring
  - need realistic fields
- Other improvements
  - Absorber shape/material, magnet arrangement
  - Matching to a complete cooling channel...
- Concerns
  - Smallest ring too small, B too high (peak  $\sim 15\text{T}$ )

# Conclusion

- Based on simplifying assumptions – the Guggenheim RFOFO works well
- Still a lot of work to do